## NORMAL COORDINATE ANALYSIS OF iNFRARED AND RAMAN SPECTRA OF SYNDIOTACTIC POLY(METHYL METHACRYLATE)

## Jifi DYBAL

Institute of Macromolecular Chemistry, Czechoslovak Academy of Sciences, 162 06 Prague 6

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Infrared and Raman spectra of crystalline syndiotactic poly(methyl methacrylate) have been analyzed by normal coordinate calculations, using a combined valence force field transferred from branched hydrocarbons and from methyl acetate. Calculations have been done for a single chain all-*trans* backbone structure of *syndiotactic* poly(methyl methacrylate) with parallel and antiparallel side-group orientations. The infrared and Raman bands observed can be satisfactorily interpreted on the basis of the calculated potential energy distributions. The best agreement between the calculated and experimental spectra has been found for the alternate cis and trans mutual orientations of the C= $O$  and C- $CH_3$  bonds in subsequent monomeric units.

Results of infrared and Raman spectroscopic studies of syndiotactic poly(methyl methacrylate) (s-PMMA) have been presented in several papers<sup>1-9</sup>. Isotopic derivatives of s-PMMA were used in the interpretation of the methyl and methylene stretching and bending vibrations<sup>1-3</sup>. The temperature dependent bands in the infrared spectra of s-PMMA in bulk and in solution were tentatively assigned to various skeletal and side-group conformations<sup>4-6</sup>. Characteristic crystalline bands were determined<sup> $7-9$ </sup> in the infrared spectra of partially crystalline s-PMMA samples obtained by the solvent induced crystallization<sup>7,10,11</sup>. However, the infrared and Raman spectra of s-PMMA have not been fully interpreted yet.

In a recent paper<sup>12</sup>, a normal-mode analysis was used for studying the vibrational spectra of isotactic PMMA. On the basis of the potential energy distributions, infrared and Raman bands over the entire spectral region could be satisfactorily interpreted and a comparison of observed infrared and Raman bands with calculated frequencies supported the  $10/1$  helical conformation of crystalline *isotactic* PMMA. In this paper we present additional experimental results (Raman spectra) and a normal-mode analysis of the vibrational spectra and structure of crystalline s-PMMA.

X-ray diffraction and infrared dichroism of partially crystalline s-PMMA samples prepared by the solvent-induced crystallization indicate<sup>7,10,11</sup> that s-PMMA chains in the crystalline phase assume a helical conformation of large radius (a fourfold

helix with 74 monomeric units in a fibre period<sup>11</sup>). The results of NMR and infrared spectroscopy suggest the formation of double helices during the self-aggregation of s-PMMA in solution<sup>9,13</sup> and <sup>13</sup>C MAS NMR spectra<sup>14</sup> support an assumption<sup>7</sup> that double-helical structures also occur in crystalline s-PMMA. All these helical structures can be generated by s-PMMA chains with a nearly extended chain conformation of the backbone; according to the conformational energy calculations, the *tt* state of a racemic diad is the most favoured<sup>15,16</sup>. Therefore, in our normal--mode analysis based on the valence force constants refined for branched hydrocarbons<sup>17</sup> and for methyl acetate<sup>18</sup> the backbone structure of the s-PMMA chain was approximated by the *tt* staggered form. The calculations were performed using model structures of s-PMMA with both parallel and antiparallel orientations of ester side-groups.

### EXPERIMENTAL

The tacticity of the s-PMMA sample studied was determined on the basis of proton NMR spectra; the content of *syndiotactic*, *heterotactic* and *isotactic* triads was 89.5, 8.5 and 2%, respectively. Partially crystalline s-PMMA was obtained by the solvent induced crystallization<sup>7-11</sup>. Samples were prepared by casting toluene and acetonitrile solutions on an aluminum foil followed by room temperature evaporation of the solvent under vacuum. Raman spectra were obtained with a Coderg LRDH 800 spectrometer. The spectra were excited by the 5145 nm line of a Coherent CR-3 laser.

## RESULTS AND DISCUSSION

The normal-mode calculations were done on a regular single chain all-trans structure of s-PMMA; the interchain forces in the double helical crystalline structure are weak compared to the intrachain ones and do not influence the frequencies significantly<sup>12</sup>. A structural repeat unit of the s-PMMA chain formed by two monomeric units is shown in Fig. 1. In the normal-mode calculations, the following bond lengths and bond angles were used:  $CC^{\alpha} = C^{\alpha}C = C^{\alpha}C^{\beta} = 0.153$  nm,  $C^{\alpha}C^* = 0.151$  nm,  $CH = 0.109$  nm,  $C^*O^* = 0.121$  nm,  $C^*O = 0.134$  nm,  $OC = 0.146$  nm,  $C^*C^*O^* = 127^{\circ}$ ,  $C^{\alpha}C^*O = 122^{\circ}$ ,  $C^*OC = 117^{\circ}$ , and the es be in the planar conformation. The structural parameters of the ester group were taken from the *ab initio* optimization of the methyl acetate molecular geometry<sup>19</sup>. The main-chain torsional angles in the suggested structures of crystalline  $s$ -PMMA<sup>10,11</sup> are shifted from perfect staggering by 10 to  $20^{\circ}$  and according to the results of the conformational energy calculations of racemic PMMA diads, the skeletal bond angles are appreciably distorted relative to the tetrahedral value (the angle  $C^{\alpha}CC^{\alpha}$  is  $\sim 124^{\circ}$ ). In the present calculations, however, we used empirical valence force fields derived for the branched hydrocarbons<sup>17</sup> and for methyl acetate<sup>18</sup> on the assumption that the corresponding bond angles are tetrahedral and that values used for

dihedral angles represent staggered or nearly staggered conformations. To ensure transferability of the force constants, these values for the structural parameters must therefore be used in the normal coordinate analysis<sup>12</sup>.

Cartesian coordinates were calculated for the ideal all-trans backbone structure of the isolated s-PMMA chain. The local symmetry coordinates were constructed from the internal coordinates defined in the standard way<sup>12</sup>. According to the conformational energy calculations<sup>16</sup>, there are two stable conformations of the side--groups in s-PMMA with cis and trans mutual orientations of the  $C=O$  and  $C -CH<sub>3</sub>$  bonds. Normal-mode calculations were performed for all three different structures of the extended s-PMMA chain defined by the stable conformations of the ester side-groups: cis—cis, cis—trans, trans—trans. The line group of the isolated  $s-PMMA$  chain with the side-chain conformations  $cis-cis$  or trans-trans is isomorphous to the point group  $C_{2v}$ . There are 86 optically active fundamental vibrations which are distributed among the symmetry species in the following manner:  $25 A_1$ , 18  $A_2$ , 18  $B_1$  and 25  $B_2$ . All the normal modes are Raman active but the  $A_2$  modes are infrared inactive.  $B_1$  modes show parallel infrared dichroism,  $A_1$  and  $B_2$  modes show perpendicular infrared dichroism. There are no nontrivial symmetry elements associated with the line group for the s-PMMA zigzag chain with cis—trans side-chain conformations. Hence, the 86 optically active fundamental vibrations are both infrared and Raman active.

Raman spectra of the solid s-PMMA samples prepared by the room temperature evaporation of the solvent from toluene solution (partially crystalline<sup>8</sup>) and from



FIG. 1 FIG. 2



Structural unit of s-PMMA Raman spectra of s-PMMA: a amorphous sample; b partially crystalline sample.  $\times$ indicates peaks due to solvent

acetonitrile solution (amorphous<sup>8</sup>) are shown in Fig. 2. Similarly to the case of the infrared spectra<sup> $7-9$ </sup>, several differences can be observed between the Raman spectra of crystalline and amorphous s-PMMA, characteristic of a transition from unordered to ordered polymer. Some of the bands in the Raman spectrum of crystalline s-PMMA show frequency shifts and changes in intensity, e.g., the band at 910 cm<sup>-1</sup> is shifted to 915 cm<sup>-1</sup> and the intensity of the band at 877 cm<sup>-1</sup> is appreciably higher in the spectrum of crystalline s-PMMA. In the spectrum of the crystalline form, a new weak band at  $275 \text{ cm}^{-1}$  appears that is not observed in the spectrum of the amorphous sample.

• The observed Raman and infrared band frequencies of crystalline s-PMMA are listed in Table I. The experimental infrared frequencies are taken from our spectra published previously<sup>8</sup>. The infrared dichroism data given in Table I are taken from the papers of Nagai' and of Kusuyama et al.7. No polarization results are available for the Raman spectra because the measured samples have defined orientation.

According to the calculations of the conformational energies of the s-PMMA chain<sup>16</sup>, three different stable conformational states defined by the ester side-group orientations are accessible to the racemic diad in the tt skeletal conformation. The lowest value of the total energy was found for the state with the *cis* positions of the C=O and  $C^{\alpha}$ - $C^{\beta}$  bonds in both monomeric units (cis-cis). The states with the  $cis$ -trans and trans-trans side-group orientations are higher in energy by  $4.8$ and  $8.0 \text{ kJ} \text{ mol}^{-1}$ , respectively. Normal mode calculations have been performed for all the three structures.

Calculated frequencies of modes above  $1\,400\,\mathrm{cm}^{-1}$  corresponding to the localized vibrations differ for these structures by less than  $1 \text{ cm}^{-1}$ ; significant differences appear in the range below  $1\,400\,\mathrm{cm}^{-1}$ . Calculated frequencies of selected vibrations of the extended s-PMMA chain with the cis-cis, cis-trans and trans-trans side--group orientations are listed in Table II and compared with the observed infrared and Raman band frequencies. In this table we list only modes above  $200 \text{ cm}^{-1}$ for which the calculated frequencies differ by  $5 \text{ cm}^{-1}$  or more. As can be seen from Table II, the calculated frequencies of the cis-trans state are in the best agreement with the bands observed. The average difference between the observed and calculated frequencies is  $8.6 \text{ cm}^{-1}$  for the *cis-trans* structure compared to 15.9 and 21.2 cm<sup>-1</sup> for the cis—cis and trans—trans structure, respectively (the average difference for the cis-trans structure over the spectral range  $1800-200$  cm<sup>-1</sup> is 9.3 cm<sup>-1</sup>). These results suggest that in the crystalline phase the ester side-groups of adjacent chemical repeat units have antiparallel orientation. Conformational energy calculations showing that the parallel cis-cis structure is more favourable were performed for the isolated racemic diad. However, s-PMMA chains in the crystalline state form a double helix<sup>7,9,13,14</sup> stabilized by intermolecular interactions not taken into account in the conformational calculations. Strong interactions of the ordered ester groups in crystalline s-PMMA are manifested in the splittings of the carbonyl

# Syndiotactic Poly(methyl methacrylate) 1657

## TABLE I

Observed and calculated frequencies (in  $cm^{-1}$ ) of syndiotactic poly(methyl methacrylate)



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# TABLE I

(Continued)



bands in the infrared and Raman spectra<sup>8,9</sup>. The preference of structures with antiparallel orientations of the side-groups in crystalline s-PMMA is most likely due to cooperative intermolecular interactions of ester groups.

Our normal coordinate analysis of the spectra of crystalline s-PMMA is based on the model structure with all-trans backbone conformations and antiparallel esters. The calculated frequencies are listed in Table I together with the potential energy distributions (PED). The s-PMMA zigzag chain with parallel esters has the  $C_{2v}$  symmetry; the structure with antiparallel ester has the  $C_1$  symmetry and all the modes belong to one type of symmetry species. However, this structure differs from the  $C_{2v}$  symmetry structure only by the rotation of one of the ester side-groups in the racemic diad. Therefore, the vibrational modes associated predominantly



TABLE II

 $\leftarrow$ 

Observed and calculated frequencies (in  $cm^{-1}$ ) of selected vibrations of *syndiotactic* poly(methyl methacrylate)

<sup>a</sup> Infrared bands:  $\sigma$  indicates electric vector perpendicular to the chain axis.  $\delta$  Calculated frequencies for the following side-group structures: trans–trans  $(I)$ , cis-trans  $(II)$ , cis-cis  $(III)$ . C PED for the structure with parallel esters (cis-cis) is given (only contributions of  $10\%$  or greater are included): s stretch, b bend, ib in-plane-bend, d deformation, r rock, t twist.

a Infrared bands:  $\pi$  indicates electric vector along the chain axis,  $\sigma$  indicates electric vector perpendicular to the chain axis.  $\bar{b}$  PED (only contributions of 10% or greater are included): s stretch, as antisymmetric stretch, ss symmetric stretch, b bend, ab antisymmetric bend, sb symmetric bend, ib in-plane bend, ob out-of-plane bend, d deformation, r rock, w wag, t twist, tor torsion.

with motions of atoms not belonging to ester groups practically preserve the symmetry behaviour of the parallel structure  $(C_{2v}$  symmetry). In Table I, symmetry types of the corresponding vibrations of the s-PMMA chain with parallel esters (cis—cis) are given for all calculated frequencies. The calculated frequencies and PEDs of several pairs of localized vibrations are practically identical. Therefore, in Table I such modes are given in one line where the two symbols of the corresponding symmetry species are included.

Assignments of the observed bands to the calculated modes were made on the basis of extensive spectral studies of isotopic derivatives of  $s$ -PMMA<sup>1-3</sup> as well as the infrared dichroism data<sup>1,7</sup>. The proposed assignments were correlated with the results of our normal-mode analysis of isotactic PMMA12.

As can be seen in Table I, the results of the normal-mode analysis suggest a reasonable interpretation of the observed bands in the C—H stretch region, from 3 100 to 2 800 cm<sup> $-1$ </sup>. The calculated PEDs are in a qualitative agreement with the results of studies of deuterated s-PMMA<sup>1,2</sup>. The observed splitting of the C=O stretch mode  $(1740 \text{ and } 1731 \text{ cm}^{-1})$  can be explained by resonance transition dipole coupling interactions<sup>9</sup>. These interactions were not included in the present calculations of the isolated s-PMMA chain.

The region from 1 500 to 1 350 cm<sup>-1</sup> contains symmetric and asymmetric bend modes of methyl and methylene groups. The infrared band at  $1\,340\,\mathrm{cm}^{-1}$  and the Raman band at 1 326 cm<sup> $-1$ </sup> correspond essentially to CH<sub>2</sub> wag modes.

Similarly to the case of *isotactic* PMMA<sup>12</sup>, the region from 1 300 to 1 150 cm<sup>-1</sup> consists of mixed modes that are highly coupled along the chain. Frequencies of the bands observed at 1 278 and 1 242  $cm^{-1}$  are very sensitive to the side-chain orientations (Table II). The weak band found at  $1.107 \text{ cm}^{-1}$  in the infrared spectrum is not predicted by the normal-mode calculations. We suppose that this band belongs to a combination, probably  $596(A_1) + 492(A_1)$ . The localized OCH<sub>3</sub> rock 2 modes of s-PMMA are predicted at the same frequencies  $(1\ 128\ \text{cm}^{-1})$  as for *isotactic* PMMA<sup>12</sup>. The assignments of the observed bands in the  $1000-900$  cm<sup>-1</sup> region to the OCH<sub>3</sub> and  $\alpha$ CH<sub>3</sub> rock vibrations<sup>1-3</sup> are essentially confirmed by the normal vibrational analysis. However, the calculated PEDs indicate large contributions from 0—C stretch and skeletal C—C stretch vibrations.

The characteristic bands of the crystalline phase of  $s$ -PMMA observed at 863 cm<sup>-1</sup> in the infrared spectrum and at  $876 \text{ cm}^{-1}$  in the Raman spectrum correspond to the  $C^{\alpha}C^{\beta}$  stretch vibration interacting with the CH<sub>2</sub> rock vibration. These bands are due to a long sequence of tt skeletal conformations. Another band observed at 843  $\text{cm}^{-1}$  corresponds to the same mode for a structure containing gauche conformations<sup>8</sup>.

On the basis of the spectra of deuterated derivatives, the bands observed at 747 and  $736 \text{ cm}^{-1}$  in the infrared and Raman spectra, respectively, were assigned to

the CH<sub>2</sub> rock vibrations<sup>1,2</sup>. However, the calculated PED indicate that, similarly to the case of isotactic PMMA'2, these bands correspond predominantly to the  $C=O$  out-of-plane bend. The doublet observed near 500 cm<sup>-1</sup> is not reproduced by the normal-mode calculations. It is probably due to a Fermi resonance between the fundamental mode calculated at  $492 \text{ cm}^{-1}$  (A<sub>1</sub>) and the combination mode  $346(A_1) + 166(A_1).$ 

Vibrational modes in the low-frequency region below  $400 \text{ cm}^{-1}$  are highly mixed and are very difficult to assign. Vibrations in this region involve coupling of the backbone and ester group bends and torsions.

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